

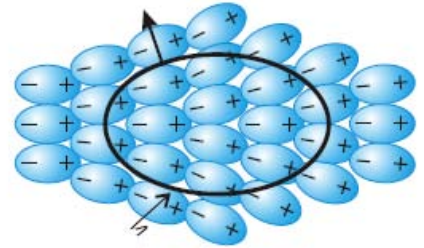
Electro-optic Modulator

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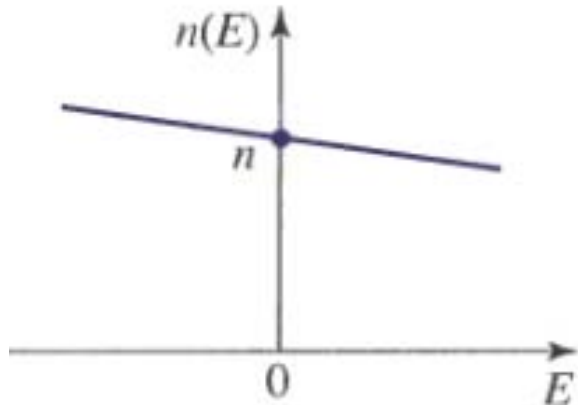
Electro optic modulator

Electro-optic Effect : Application of electric field results in redistribution of charges thus changing the refractive index of a material and thereby the effect on polarized light transmitting through it.



$$n(E) = n + aE + \frac{1}{2}bE^2 + \dots$$

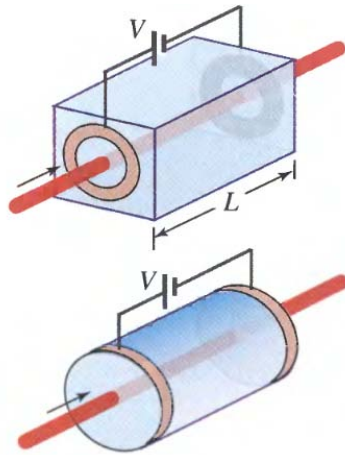
Pockels Effect : The refractive index changes linearly with the applied electric field.



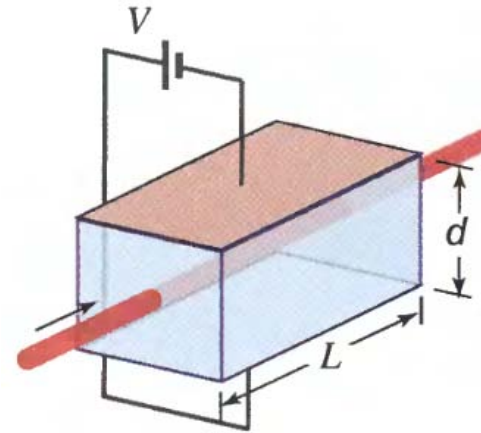
Pockels Effect : the linear Electro-optic effect.



Friedrich Pockels described the linear Electro-optic effect in 1893.



Longitudinal



Transverse

Applications:

- Lens of controllable focal length.
- Optical scanning devices.
- Controllable wave retarder.
- Intensity modulator or optical switch.
- Fast optical shutters.

Crystal Optics: EM Wave in Anisotropic Medium

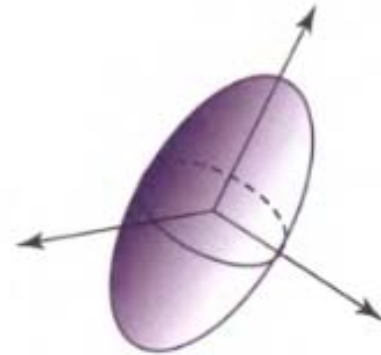
In linear anisotropic dielectric medium electric flux density is related to electric field as

$$D_i = \sum_j \varepsilon_{ij} E_j \quad i, j = 1, 2, 3$$

refer to x, y, z components.

An ellipsoid is a quadratic surface, geometrical representation of a symmetric second rank tensor,

$$\sum_{ij} \varepsilon_{ij} x_i x_j = 1$$



The coordinate system for which dielectric tensor is diagonal defines the principal axes and the principal planes of the crystal, D and E are parallel

$$D_1 = \varepsilon_1 E_1 \quad , \quad D_2 = \varepsilon_2 E_2 \quad , \quad D_3 = \varepsilon_3 E_3$$

where,

$$\varepsilon_1 = \varepsilon_{11} \quad , \quad \varepsilon_2 = \varepsilon_{22} \quad , \quad \varepsilon_3 = \varepsilon_{33}$$

and

$$n_1 = \sqrt{\varepsilon_1 / \varepsilon_0} \quad , \quad n_2 = \sqrt{\varepsilon_2 / \varepsilon_0} \quad , \quad n_3 = \sqrt{\varepsilon_3 / \varepsilon_0}$$

Electric impermeability tensor

$$\eta = \varepsilon_0 \varepsilon^{-1}$$

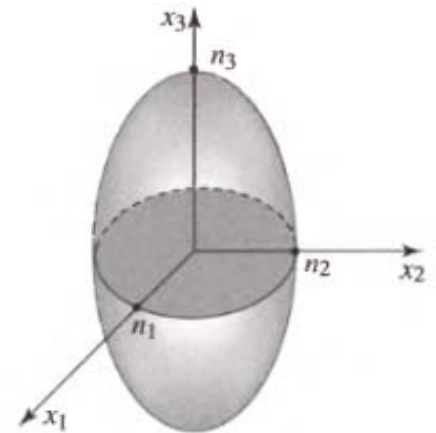
is diagonal in principal coordinate system.

Index ellipsoid is the quadratic representation of the electric impermeability tensor

$$\sum_{ij} \eta_{ij} x_i x_j = 1 \quad i, j = 1, 2, 3$$

If the principal axes are used as coordinate system, for convenience, $x = 1, y = 2, z = 3$

$$\frac{x^2}{n_x^2} + \frac{y^2}{n_y^2} + \frac{z^2}{n_z^2} = 1$$



Since, refractive index is a function of applied field, the optical impermeability tensor, $\eta_{ij}(E)$ is modified.

$$\Delta \eta_{ij} = \Delta(1/n^2)_{ij} = r_{ijk} E_k, \quad k = x, y, z$$

The coefficients r_{ijk} are called the Pockels Coefficient.

Index ellipsoid is modified

$$\eta_{ij}(E)x_i x_j = 1$$

or

$$\left(\frac{1}{n_x^2} + r_{11k} E_k\right)x^2 + \left(\frac{1}{n_y^2} + r_{22k} E_k\right)y^2 + \left(\frac{1}{n_z^2} + r_{33k} E_k\right)z^2 + 2yzr_{23k} E_k + 2zxr_{13k} E_k + 2xyr_{12k} E_k = 1$$

Mixed terms; Principal axes of crystal x, y, z are no longer principal axes of index ellipsoid.

Using contracted indices,

$j \setminus i$	1	2	3
1	1	6	5
2	6	2	4
3	5	4	3

$$\left(\frac{1}{n_x^2} + r_{1k} E_k\right)x^2 + \left(\frac{1}{n_y^2} + r_{2k} E_k\right)y^2 + \left(\frac{1}{n_z^2} + r_{3k} E_k\right)z^2 + 2yzr_{4k} E_k + 2zxr_{5k} E_k + 2xyr_{6k} E_k = 1$$



Electro-optic tensor for ADP crystal is

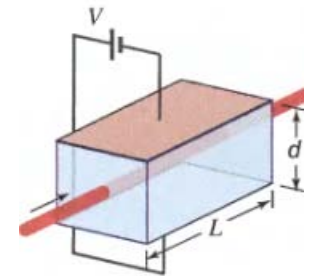
$$r_{ij} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ r_{41} & 0 & 0 \\ 0 & r_{41} & 0 \\ 0 & 0 & r_{63} \end{pmatrix}.$$

the modified index ellipsoid is

$$\frac{x^2}{n_x^2} + \frac{y^2}{n_y^2} + \frac{z^2}{n_z^2} + 2y z r_{41} E_x + 2z x r_{41} E_y + 2x y r_{63} E_z = 1$$

ADP is uniaxial and in transverse mode,

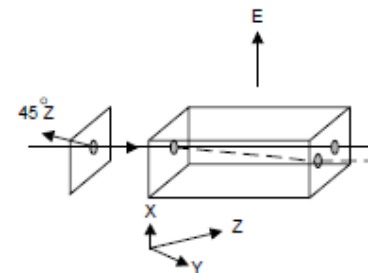
$$\frac{x^2}{n_0^2} + \frac{y^2}{n_0^2} + \frac{z^2}{n_e^2} + 2y z r_{41} E_x = 1$$



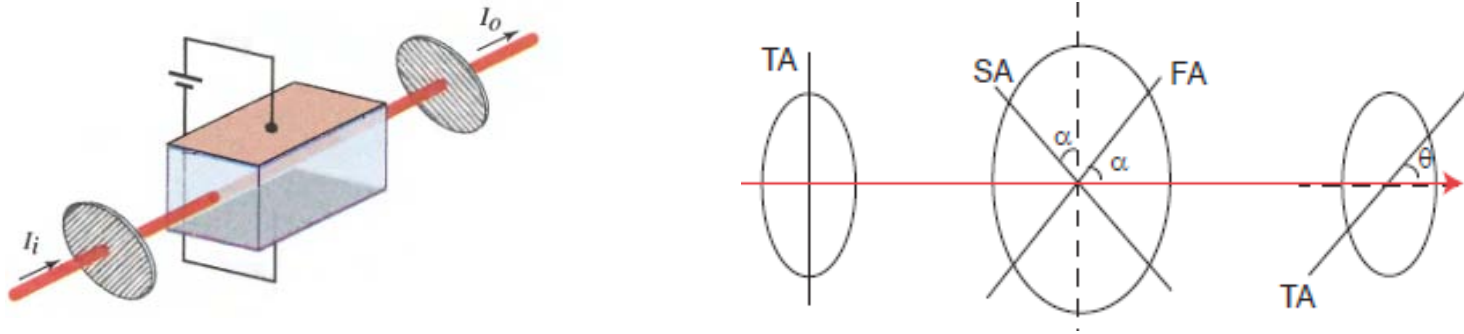
The phase retardation, Γ between normal modes is,

$$\Gamma = \frac{2\sqrt{2}}{(1/n_0^2 + 1/n_e^2)^{3/2}} r_{41} \frac{\pi V}{\lambda d} L$$

$$\Gamma = \frac{\pi V}{V_\pi}$$



Transmission curves for Pockels cell :



$$I_o = I_i/4 (2 - \text{Cos}[4\alpha - 2\theta] - \text{Cos}[2\theta] - 2 \text{Cos}[\Gamma] \text{Sin}[2\alpha] \text{Sin}[2(\alpha - \theta)])$$

For, $\alpha = \pi/4$

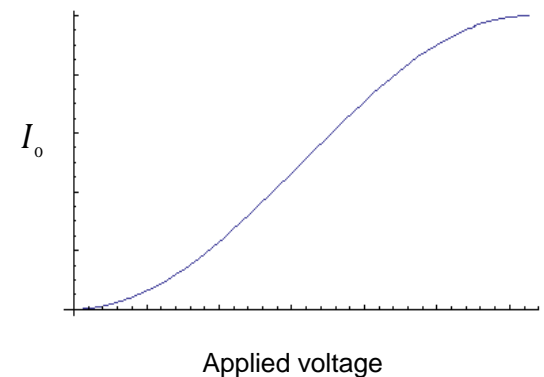
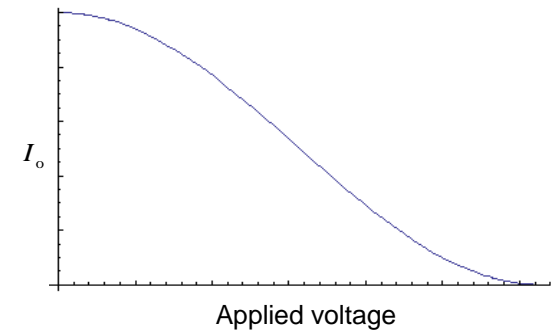
$$I_o = I_i/2 (1 - \text{Cos} 2\theta \text{Cos} \Gamma)$$

For parallel polarizer, $\theta = \pi/2$

$$I_o = I_i \text{Cos}^2(\Gamma/2)$$

For crossed polarizer, $\theta = 0$

$$I_o = I_i \text{Sin}^2(\Gamma/2)$$



Amplitude modulation:

Biased at quarter wave voltage

$$I_o = I_i \text{Sin}^2\left(\frac{1}{2}\left(\frac{\pi}{2} + \Gamma_m \text{Sin}\omega_m t\right)\right)$$

$$I_o \approx \frac{I_i}{2} (1 + \Gamma_m \text{Sin}\omega_m t)$$

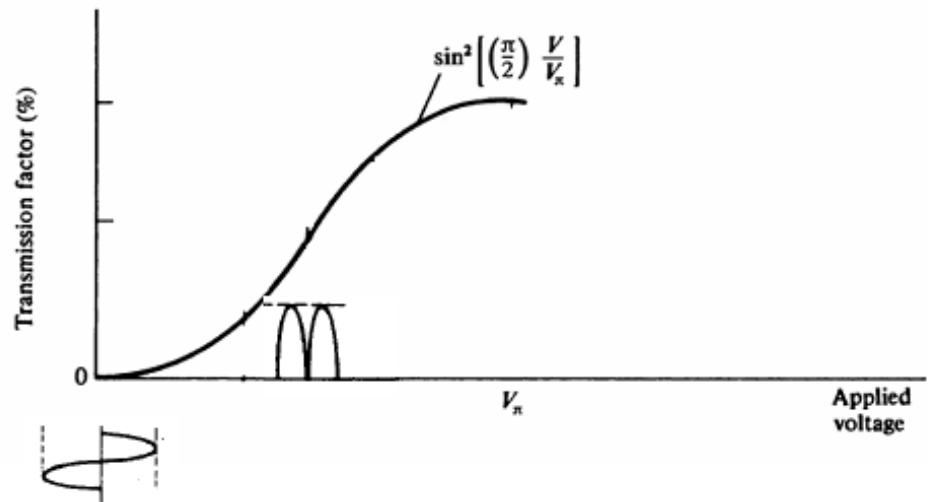
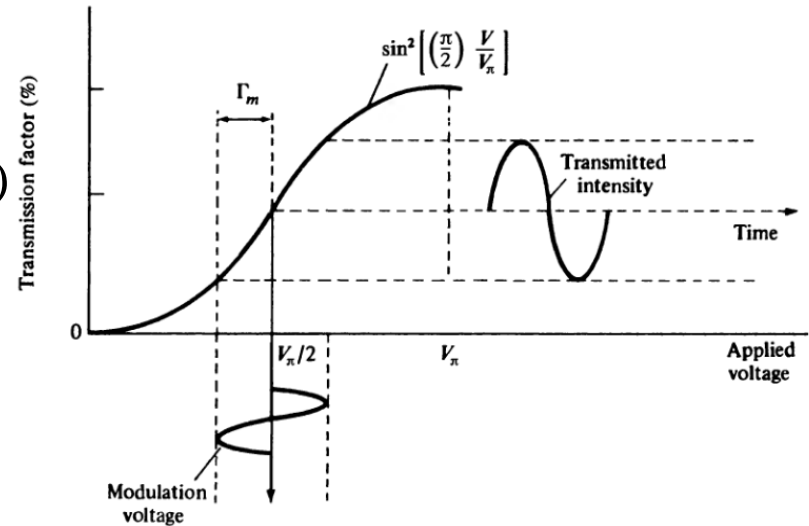
Where,

$$\Gamma_m = \pi(V_m / V_\pi)$$

Unbiased or biased at half wave voltage

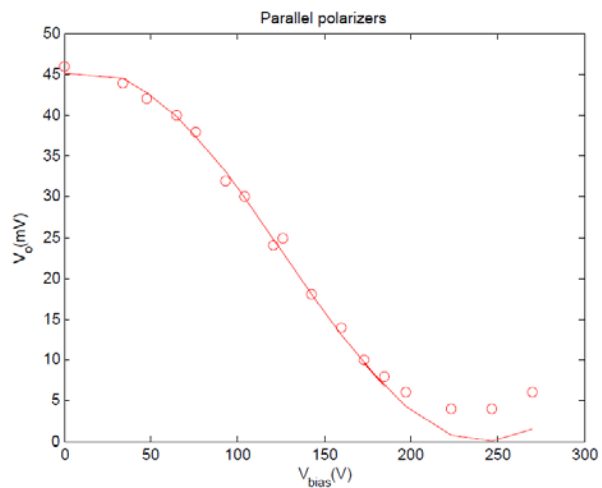
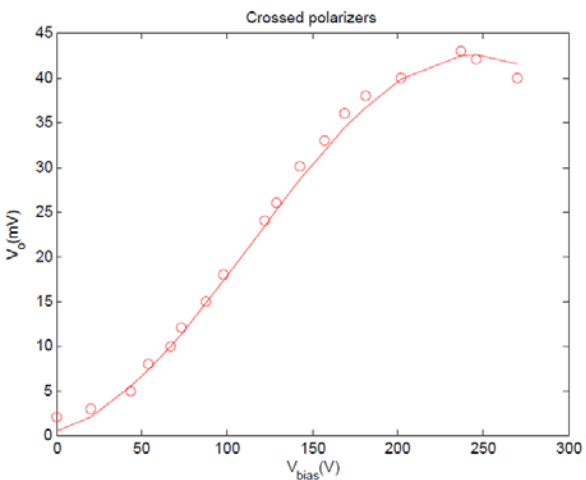
$$I_o = I_i \text{Sin}^2\left(\frac{\pi}{2V_\pi} V_m \text{Sin}\omega_m t\right)$$

$$I_o = I_i \frac{\pi^2 V_m^2}{8V_\pi^2} (1 + \text{Cos} 2\omega_m t)$$

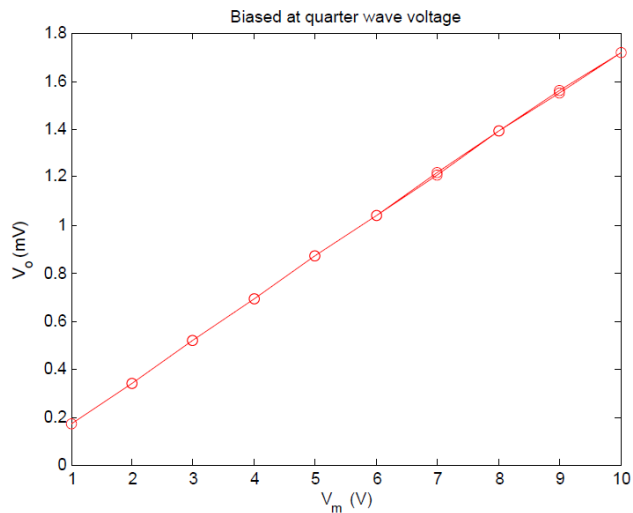
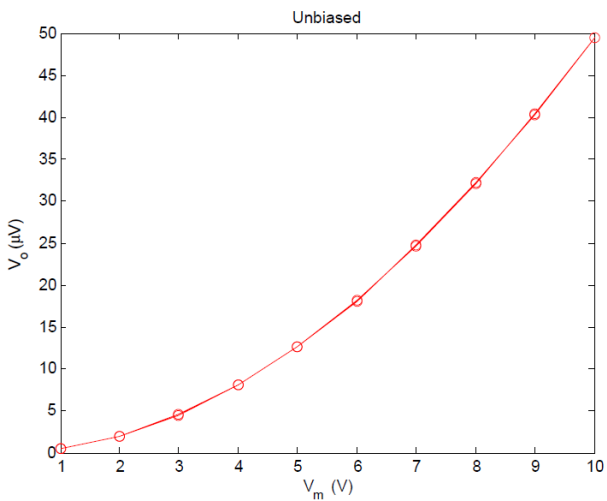


Results:

1. Transmission curves for EOM



2. Amplitude modulation



THANK YOU