

# Surface Plasmon Resonance Demo

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## Items:

- a) Polarization stabilized He-Ne laser at 633nm
- b) Equilateral Prism of known refractive index
- c) Linear Polarizer
- d) Half wave-plate @ 633nm
- e) Precision Rotation stage (0.5 degree or better)
- f) Photo-detector

## Procedure Gold Deposition:

Wipe Prism Clean with Tissue

HCL immersion for 2 minutes

Rinse with water

10 minutes immersion in acetone, followed by 10 minutes in Isopropanol then dry

Clean sputtering system with acetone. Since prism height is large and there is not enough headroom in the chamber, to accommodate the prism remove rod below the round sample holder by rotating it off (! be careful not to bend or strain the wire connected to the holder). Replace with the shorter screw/rod in the target drawer. Using the two copper supports place the prism with the deposition surface horizontal and facing the target. Deposit gold for 360seconds at 22mA current under argon gas (Denton system is open loop and measured current under stable conditions is always 2mA less than inputted current hence actual current should be 20mA).

Using acetone wipe clean the other two surfaces to remove unintended gold deposition.

The estimated gold film thickness is 50nm for given time/current.

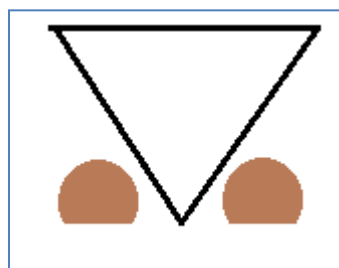


Fig 1. Prism arrangement in sputtering chamber

**Experimental Setup:**

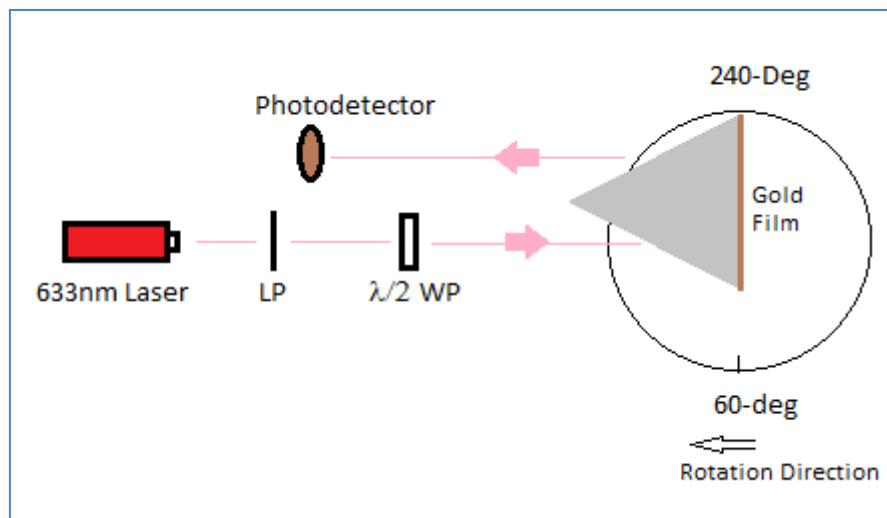


Fig 2. Setup for SPR Observation

Setup the prism onto the rotation stage such that the back face with the gold film is on the 240-60deg line and the line marker on the stage points to 60 degrees in the orientation shown in figure 2. This ensures that the angle indicated by the line marker is  $\theta_{ext}$  the external angle onto the prism face. As the stage is rotated in clockwise direction the photodetector needs to be moved manually to detect the light reflected from the back face. To check if alignment is accurate rotate the prism to zero degree position and see if the light reflected from the front surface goes directly back towards the incident beam.

Ensure that the photodetector is not saturated at the maximum reflection intensity; reduce power using the linear polarizer if needed. The SPR dip is maximized for p polarized light; use the waveplate to ensure that the beam is p or s polarized as needed.

**Results:**

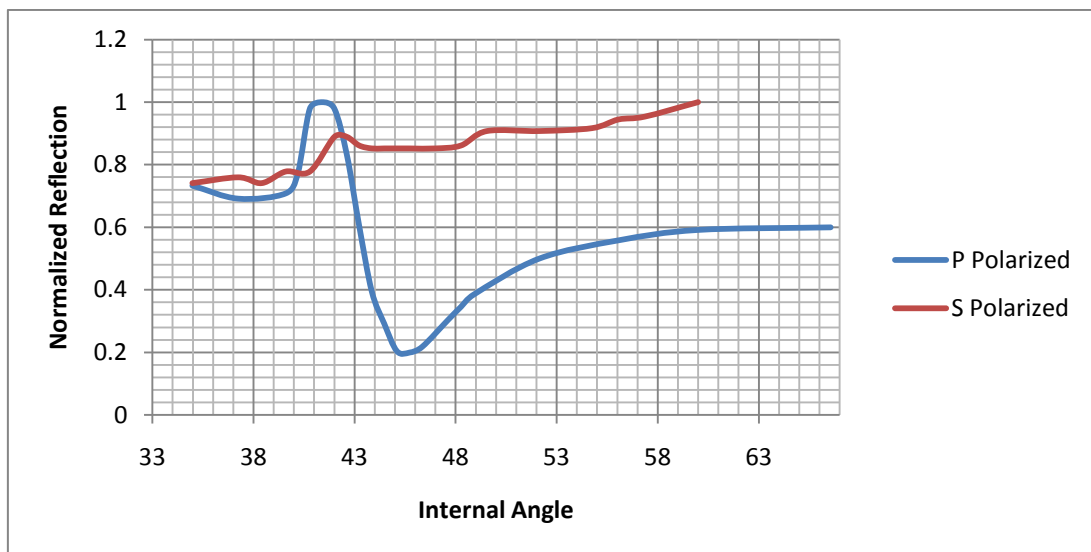


Fig 3. Reflection vs internal angle for 6minute Deposition ( Prism B)

The total internal reflection angle for glass with  $n=1.49$  is 42 degrees which corresponds to external angle of 28 degrees. This is where the reflection maximizes as shown in figure 3. Beyond that SPR dip is observed for P Polarized light only at 45 degrees.

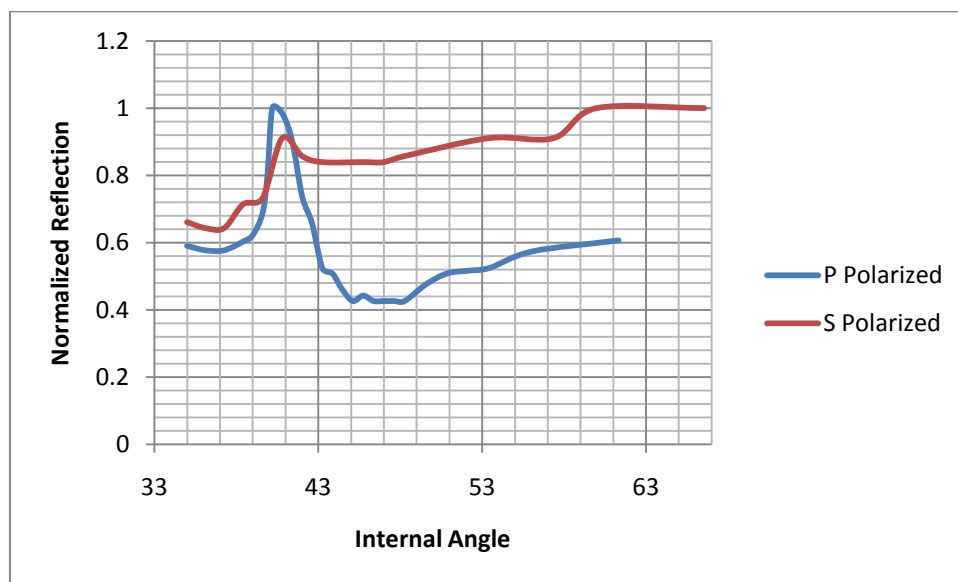


Fig 4. Reflection vs internal angle for 5minute deposition (Prism A)

Reduced dip observed for 5 minute deposition suggesting that optical film thickness was not reached at 5minutes.

**NOTE: Prism A** – 5 minutes Deposition, **Prism B** – 6 minutes deposition and **Prism C** – 9 minutes deposition

The SPR technique can be used for high sensitivity detection of molecules adsorbing onto the metallic film. To see this effect the prism was dipped in water for 5 minutes then dried in air. We deposited gold for 6 minutes on a second prism for this experiment. The SPR dip before water is slightly shifted from the results in figure 3 and 4 possibly due to different refractive index of the prism.

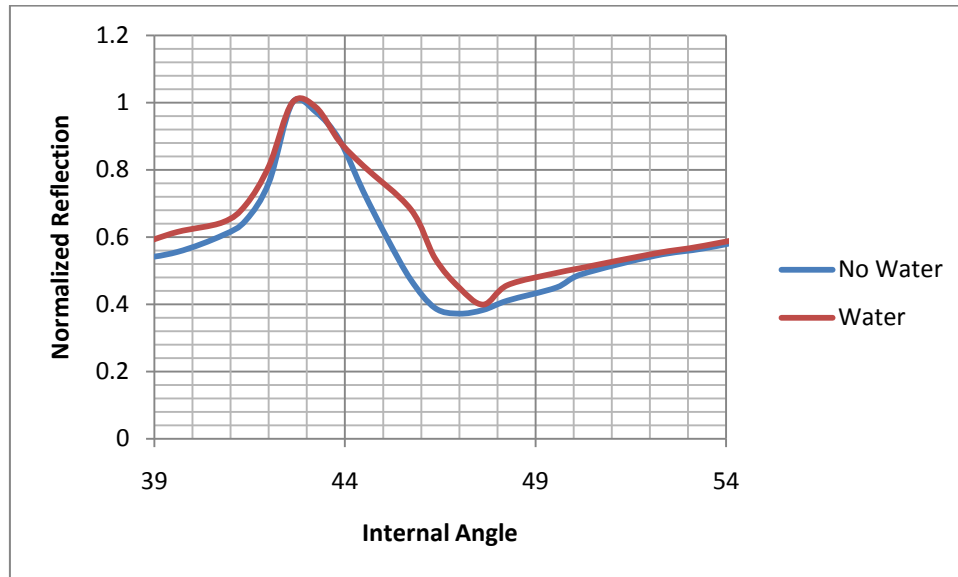


Fig 5. Effect of immersing prism in water for 5 minutes

We observe a 1 degree shift after exposure to water. From simulation results shown in figure 6 a 1 degree shift corresponds to a 10nm layer of water molecules.

More data is in appendix 3.

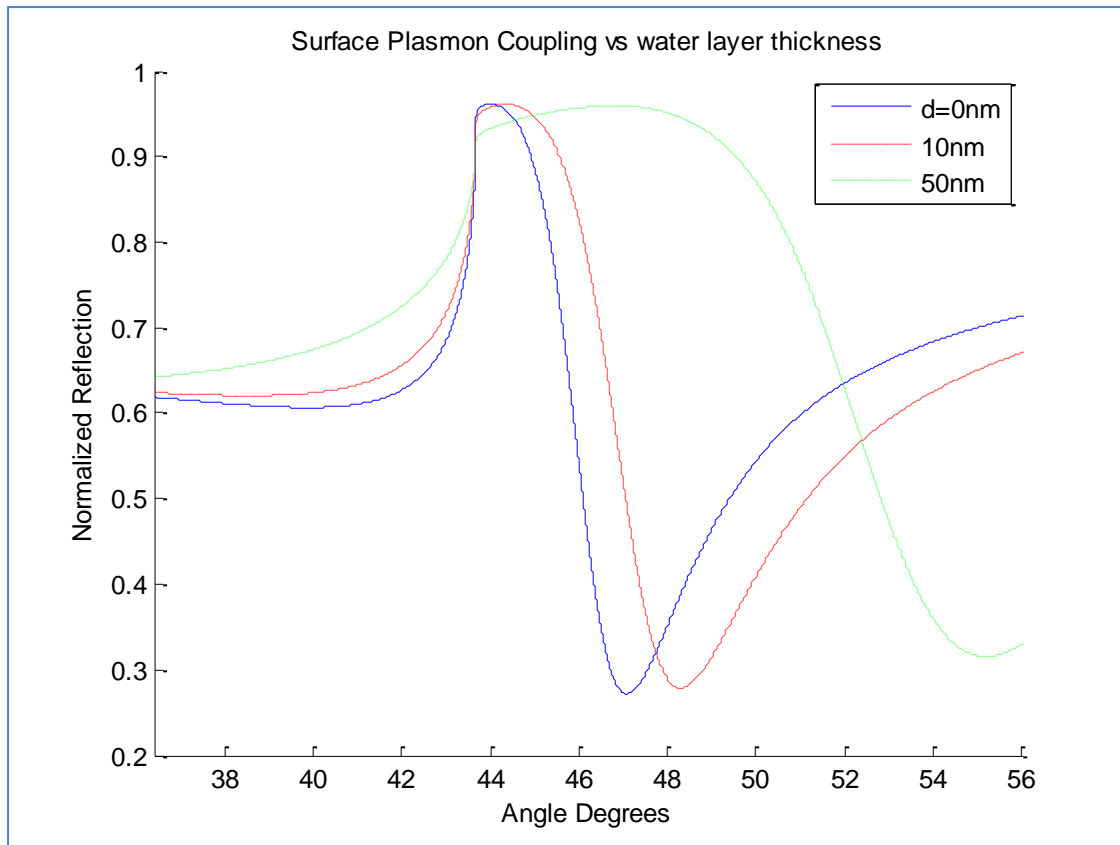


Fig 6. Simulation for different water thicknesses on gold (nprism taken to be 1.45)

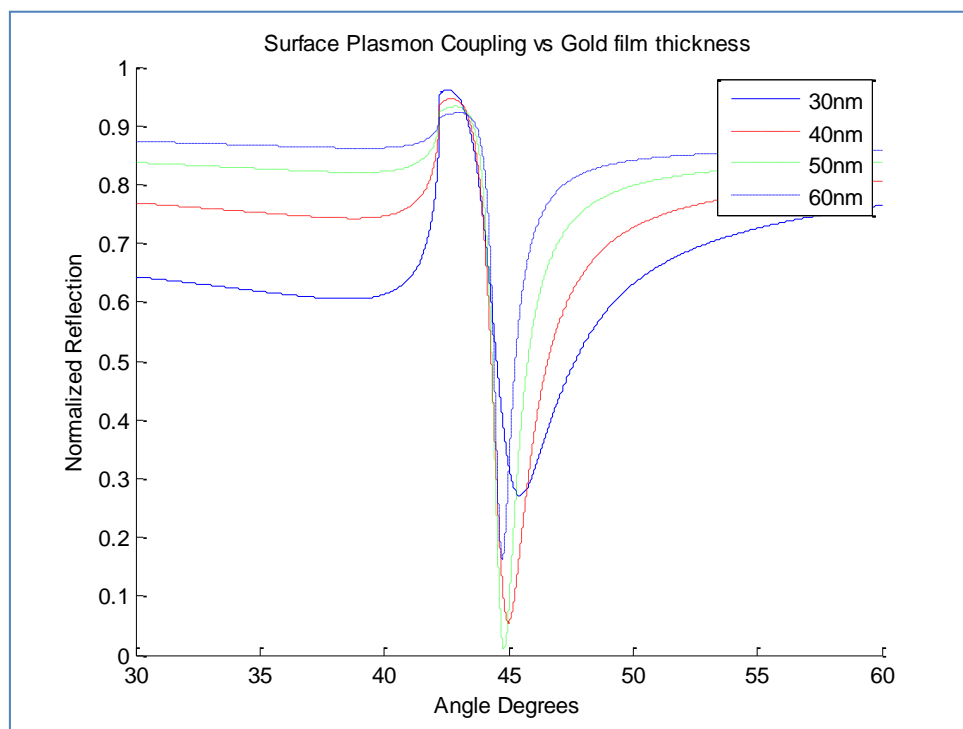


Fig 7. Effect of different gold thicknesses on SPR dip

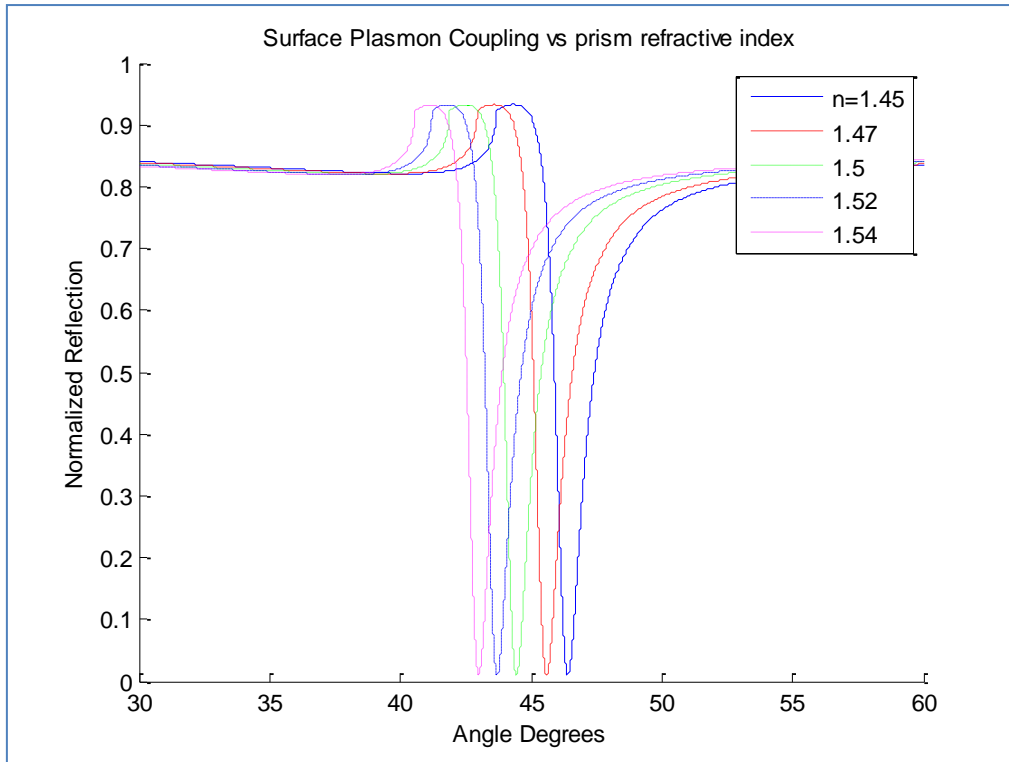


Fig 8. Effect of prism refractive index on gold.

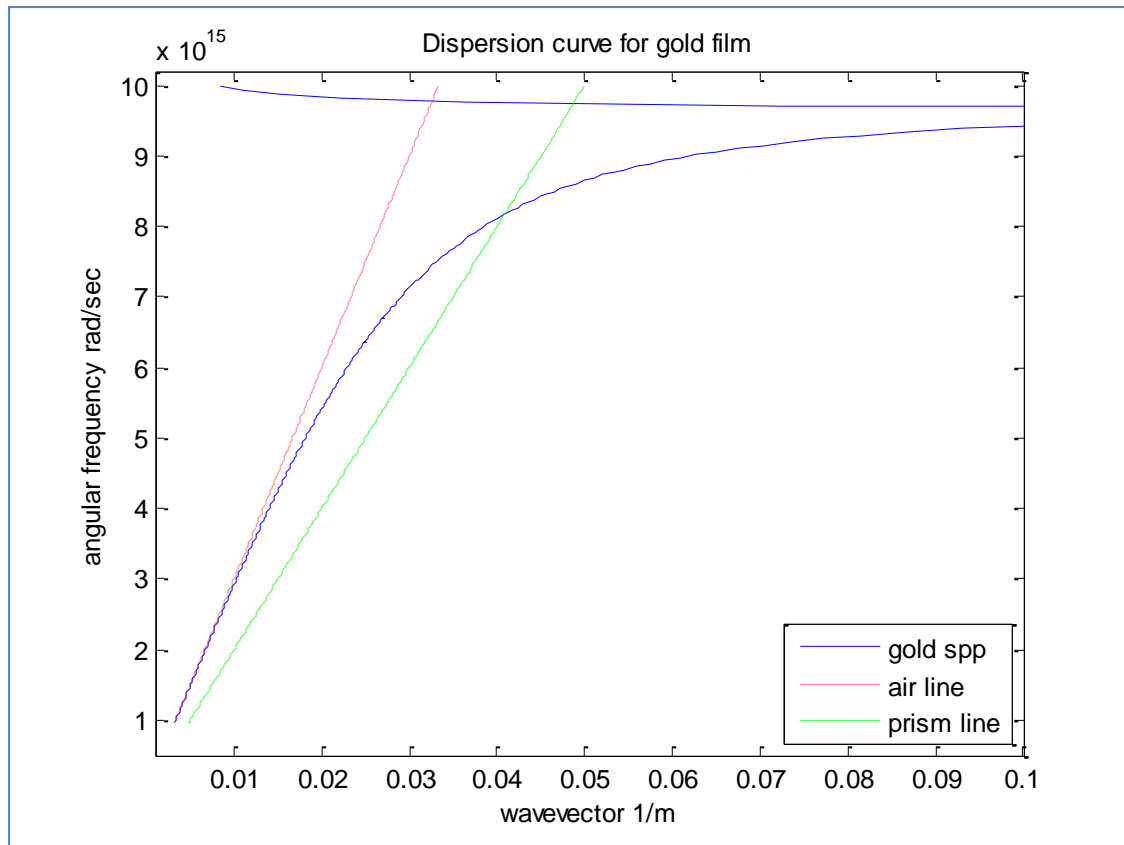


Fig 9. Dispersion curve for gold thin film

## Useful relations/theory:

- 1- **Fresnel reflection coefficient for 2 thin film system (e.g. gold/water) [Quail et al, Optics Letters 1983]:**

$$R_{1234} = \frac{r_{12} + R_{234} \exp(i2k_{2z}d_2)}{1 + r_{12}R_{234} \exp(i2k_{2z}d_2)}, \quad r_{ij} = \frac{\sqrt{\epsilon_j} \cos \theta_i - \sqrt{\epsilon_i} \cos \theta_j}{\sqrt{\epsilon_j} \cos \theta_i + \sqrt{\epsilon_i} \cos \theta_j}$$

where

and

$$R_{234} = \frac{r_{23} + r_{34} \exp(i2k_{3z}d_3)}{1 + r_{23}r_{34} \exp(i2k_{3z}d_3)}. \quad k_{iz} = \frac{\omega}{c} (\epsilon_i - \epsilon_1 \sin^2 \theta_1)^{1/2}.$$

i,j go from 1 to 4 corresponding to prism, gold, water (or other dielectric) and air respectively.

- 2- **Dispersion relation for SPR between a dielectric and a metal [Maier, Plasmonics: Fundamentals and Applications]:**

$$\beta = k_0 \sqrt{\frac{\epsilon_1 \epsilon_2}{\epsilon_1 + \epsilon_2}}.$$

- 3- **Relationship between internal and external angle of a equilateral prism for the used geometry**

$$\phi_{int} = 60 - \arcsin\left(\frac{\sin(\phi_{ext})}{n}\right)$$

$\phi_{int}$  is the internal angle on the prism/gold interface

$\phi_{ext}$  is the external angle onto the prism wrt. the surface normal

## References:

Laboratory experiments for exploring the surface Plasmon resonance, Pluchery et al, European Journal of Physics, 2011

Quantitative Interpretation of the Response of Surface Plasmon Resonance Sensors to the Adsorbed Films, S. Jung, Langmuir 1998

Long-range surface-plasmon modes in silver and aluminum films, J.C. Quail Optics Letters 1983

Magnetoplasmonic Nanostructures: systems supporting both plasmonic and magnetic properties , F Armelles, Journal of Optics A: Pure and Applied Optics, 2009

Plasmonics: Applications and Fundamentals, Maier, 2007



## Appendix - 1

```
%% SPP dispersion curve for gold thin film and light lines for air and
%% glass
close all,
clear;
nprism=1.5;
gma=1/(9e-15);
wp=2*pi*2.175e15;
lambda=189:1:1940;
eps=gold_eps(lambda);

c1=3e17;
w2=2*pi*c1./lambda;

eps2=1-((wp^2)./(w2.^2+1i*gma*w2));

beta=w2/c1.*((eps2)./(eps2+1)).^0.5;
k1=w2./c1;
plot(real(beta),w2);
hold on
plot(k1,w2,':r');
plot(k1*nprism,w2,'--g');
legend('gold spp','air line','prism line','Location','Southeast')
xlabel('wavevector 1/m');
ylabel('angular frequency rad/sec');
axis([0.001 0.1 0.5*10^15 1.02e16]);
title('Dispersion curve for gold film')
lmda=2*pi*c1/8.15e15 %intersection of gold spp with prism ie max possible
wavelength
%figure
%plot(lambda,real(eps));
%figure
%plot(lambda,imag(eps));
```

## Appendix - 2

```
% Fresnel Reflection Calculations for gold thin film on glass prism%
clc
clear
close all
dgold=50e-9;
dwater=0e-9;
nprism=1.49;
lmda=633e-9; %% laser wavelength

epsi(4)= 1; %air
epsi(3)= 1.33^2; % liquid (water)
epsi(2)=gold_eps(lmda*10^9); %%gold_eps is a function that gives the
dielectric constant for gold for a given lmda (download from mathwork
website)
epsi(1)=nprism^2; %prism/substrate

div=1000; %% no. of points
d(1)=dgold; %gold layer
d(2)=dwater; % water layer thickness
```

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```
rngel=35; %angle start range
rngel2=60; %angle end range

thetain=rngel:(rngel2-rngel)/div:rngel2; %internal angle

    theta(1,:)=thetain;

for i=1:3

theta(i+1,:)=(asin(sqrt(epsil(i)).*sin(theta(i,:)*3.14/180)./sqrt(epsil(i+1))
))*180/pi; %% rest of the angles in each layer
end

for i=1:3
    r(i,:)=(sqrt(epsil(i+1))*cos(theta(i,:)*3.14/180)-
sqrt(epsil(i))*cos(theta(i+1,:)*3.14/180))./(sqrt(epsil(i+1))*cos(theta(i,:)*
3.14/180)+sqrt(epsil(i))*cos(theta(i+1,:)*3.14/180));
end

for i=1:3
    k(i,:)=(2*pi/lmda)*(epsil(i)-
epsil(1)*(sin(theta(1,:)*3.14/180).^2)).^0.5; %wavevectors for each layer
end

R2=(r(2,:)+r(3,:).*exp(1i*2.*k(3,:)*d(2)))./(1+r(2,:).*r(3,:).*exp(1i*2*k(3
,:)*d(2))); %% reflection coeffecient for layer 2 to 4

R1=(r(1,:)+R2.*exp(1i*2.*k(2,:).*d(1)))./(1+r(1,:).*R2.*exp(1i*2.*k(2,:).*d
(1)));%% reflection for total stack

ref=sgolayfilt(abs(R1),1,15);
plot(theta(1,:),(abs(R1)).^2);
grid on
xlabel('Internal angle deg')
ylabel('Normalized Reflection')
```

### Appendix - 3 - READINGS

#### P Polarized on glass slide with 6 minute deposition

theta	thetain	theta	pdiode mV	Normalized
20	40	34.98304	236	0.813793103
23	37	36.67595	244	0.84137931
24	36	37.25063	248	0.855172414
26	34	38.41445	256	0.882758621
28	32	39.59639	264	0.910344828
30	30	40.7951	288	0.993103448
31	29	41.40034	288	0.993103448
32	28	42.00928	280	0.965517241
33	27	42.62178	272	0.937931034
34	26	43.23769	260	0.896551724
35	25	43.85684	252	0.868965517
36	24	44.4791	240	0.827586207
37	23	45.10432	232	0.8
38	22	45.73236	236	0.813793103
40	20	46.99634	244	0.84137931
42	18	48.26996	248	0.855172414
44	16	49.55216	252	0.868965517
46	14	50.84191	256	0.882758621
48	12	52.13821	260	0.896551724
50	10	53.44008	268	0.924137931
52	8	54.74657	272	0.937931034
54	6	56.05673	276	0.951724138

**6.5 minutes P Polarized**

thetain	theta	pdiode mV	Normalized
30	40.7951	18.8	0.810344828
26	43.23769	23.2	1
25	43.85684	21.6	0.931034483
24	44.4791	16	0.689655172
23	45.10432	10	0.431034483
22	45.73236	6	0.25862069
21	46.36308	4	0.172413793
20	46.99634	2.4	0.103448276
19	47.63201	2	0.086206897
18	48.26996	2.4	0.103448276
17	48.91005	3.2	0.137931034
16	49.55216	4.4	0.189655172
14	50.84191	4.4	0.189655172
12	52.13821	6.4	0.275862069
10	53.44008	7.6	0.327586207
8	54.74657	8.8	0.379310345
6	56.05673	10	0.431034483
4	57.36963	11	0.474137931
2	58.68436	12.6	0.543103448
0	60	13.2	0.568965517

**S Polarized**

thetain	theta	pdiode mV	Normalized
40	34.98304	80	0.689655
36	37.25063	82	0.706897
34	38.41445	80	0.689655
32	39.59639	84	0.724138
30	40.7951	84	0.724138
28	42.00928	90	0.775862
27	42.62178	94	0.810345
26	43.23769	96	0.827586
25	43.85684	94	0.810345
24	44.4791	94	0.810345
22	45.73236	94	0.810345
20	46.99634	102	0.87931
18	48.26996	102	0.87931
16	49.55216	102	0.87931
12	52.13821	108	0.931034
8	54.74657	112	0.965517
6	56.05673	116	1
4	57.36963	112	0.965517
0	60	112	0.965517

**4 minutes 50 seconds P Polarized**

thetain	theta	pdiode mV	Normalized
40	34.98304	72	0.590163934
38	36.10634	70.4	0.57704918
36	37.25063	70.4	0.57704918
34	38.41445	73.6	0.603278689
33	39.00324	76	0.62295082
32	39.59639	84	0.68852459
31.5	39.89455	98	0.803278689
31	40.19373	122	1
30	40.7951	120	0.983606557
29	41.40034	110	0.901639344
28	42.00928	90	0.737704918
27	42.62178	80	0.655737705
26	43.23769	64	0.524590164
25	43.85684	62	0.508196721
24	44.4791	56	0.459016393
23	45.10432	52	0.426229508
22	45.73236	54	0.442622951
21	46.36308	52	0.426229508
20	46.99634	52	0.426229508
19	47.63201	52	0.426229508
18	48.26996	52	0.426229508
16	49.55216	58	0.475409836
14	50.84191	62	0.508196721
12	52.13821	63	0.516393443
10	53.44008	64	0.524590164
6	56.05673	70	0.573770492
-2	61.31564	74	0.606557377

**S Polarized**

thetain	theta	pdiode mV	Normalized
40	34.98304	74	0.660714
38	36.10634	72	0.642857
36	37.25063	72	0.642857
34	38.41445	80	0.714286
32	39.59639	82	0.732143
30	40.7951	102	0.910714
28	42.00928	96	0.857143
26	43.23769	94	0.839286
22	45.73236	94	0.839286
20	46.99634	94	0.839286
18	48.26996	96	0.857143
10	53.44008	102	0.910714
4	57.36963	102	0.910714
0	60	112	1
-10	66.55992	112	1

**P Polarized 9 minutes deposition**

thetain	theta	pdiod mV	Normalized
40	34.98304	76	0.678571429
38	36.10634	72	0.642857143
32	39.59639	80	0.714285714
31	40.19373	92	0.821428571
30	40.7951	108	0.964285714
29	41.40034	112	1
28	42.00928	108	0.964285714
27	42.62178	102	0.910714286
26	43.23769	90	0.803571429
25	43.85684	72	0.642857143
24	44.4791	62	0.553571429
23	45.10432	52	0.464285714
22	45.73236	44	0.392857143
21	46.36308	38	0.339285714
20	46.99634	34	0.303571429
19	47.63201	32	0.285714286
18	48.26996	30	0.267857143
17	48.91005	30	0.267857143
16	49.55216	30	0.267857143
14	50.84191	30	0.267857143
10	53.44008	30	0.267857143
4	57.36963	38	0.339285714
-2	61.31564	48	0.428571429
-10	66.55992	58	0.517857143
-14	69.15809	64	0.571428571
-20	73.00366	80	0.714285714

**S Polarized**

thetain	theta	pdiod mV	Normalized
40	34.98304	84	0.777778
30	40.7951	94	0.87037
26	43.23769	94	0.87037
22	45.73236	90	0.833333
18	48.26996	92	0.851852
10	53.44008	102	0.944444
6	56.05673	104	0.962963
0	60	106	0.981481
-4	62.63037	108	1
-10	66.55992	106	0.981481
-18	71.73004	98	0.907407

**P Polarized 6 minutes deposition**

thetain	theta	pdiode mV	Normalized
40	34.98304	70.4	0.733333333
36	37.25063	66.4	0.691666667
32	39.59639	68	0.708333333
31	40.19373	74	0.770833333
30	40.7951	94	0.979166667
29	41.40034	96	1
28	42.00928	94	0.979166667
27	42.62178	80	0.833333333
26	43.23769	58	0.604166667
25	43.85684	38	0.395833333
24	44.4791	28	0.291666667
23	45.10432	19.6	0.204166667
22	45.73236	19.2	0.2
21	46.36308	21	0.21875
19	47.63201	29.2	0.304166667
18	48.26996	33.2	0.345833333
17	48.91005	37	0.385416667
12	52.13821	48	0.5
6	56.05673	53.6	0.558333333
0	60	56.8	0.591666667
-10	66.55992	57.6	0.6

**S Polarized**

thetain	theta	pdiode mV	Normalized
40	34.98304	80	0.740741
36	37.25063	82	0.759259
34	38.41445	80	0.740741
32	39.59639	84	0.777778
30	40.7951	84	0.777778
28	42.00928	96	0.888889
27	42.62178	96	0.888889
26	43.23769	93	0.861111
25	43.85684	92	0.851852
24	44.4791	92	0.851852
22	45.73236	92	0.851852
20	46.99634	92	0.851852
18	48.26996	93	0.861111
16	49.55216	98	0.907407
12	52.13821	98	0.907407
8	54.74657	99	0.916667
6	56.05673	102	0.944444
4	57.36963	103	0.953704
0	60	108	1

**6 min prism 2-- no water**

thetain	theta	pdiode mV	Normalized
40	34.98304	100	0.471698113
38	36.10634	96	0.452830189
36	37.25063	96	0.452830189
34	38.41445	96	0.452830189
32	39.59639	108	0.509433962
31	40.19373	116	0.547169811
30	40.7951	124	0.58490566
29	41.40034	160	0.754716981
28	42.00928	212	1
27	42.62178	212	1
26	43.23769	188	0.886792453
24	44.4791	128	0.603773585
23	45.10432	96	0.452830189
22	45.73236	80	0.377358491
21	46.36308	64	0.301886792
20	46.99634	60	0.283018868
18	48.26996	60	0.283018868
17	48.91005	62	0.29245283
16	49.55216	64.8	0.305660377
14	50.84191	74	0.349056604
12	52.13821	82.4	0.388679245
10	53.44008	92	0.433962264
8	54.74657	108	0.509433962
6	56.05673	112	0.528301887
4	57.36963	118	0.556603774
2	58.68436	126	0.594339623
0	60	134	0.632075472

**6 min prism 2-- with water**

thetain	theta	pdiode mV	Normalized
40	34.98304	90	0.416667
38	36.10634	92	0.425926
36	37.25063	94	0.435185
34	38.41445	98	0.453704
30	40.7951	132	0.611111
29	41.40034	182	0.842593
28	42.00928	216	1
27	42.62178	196	0.907407
26	43.23769	176	0.814815
25	43.85684	140	0.648148
24	44.4791	104	0.481481
23	45.10432	86	0.398148
22	45.73236	76	0.351852
21	46.36308	66	0.305556
20	46.99634	66	0.305556
19	47.63201	70	0.324074
18	48.26996	70	0.324074
16	49.55216	84	0.388889
15	50.19615	84	0.388889
14	50.84191	96	0.444444
12	52.13821	112	0.518519
10	53.44008	122	0.564815
8	54.74657	126	0.583333
4	57.36963	144	0.666667
0	60	162	0.75
-2	61.31564	168	0.777778
-10	66.55992	168	0.777778



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-4	62.63037	140	0.660377358
-10	66.55992	166	0.783018868

**6 min prism 2-- no water**

thetain	theta	pdiode mV	Normalized
40	34.98304	76	0.527777778
36	37.25063	76	0.527777778
34	38.41445	76.8	0.533333333
32	39.59639	80	0.555555556
30	40.7951	87.2	0.605555556
29	41.40034	93.6	0.65
28	42.00928	110	0.763888889
27	42.62178	144	1
26	43.23769	140	0.972222222
25	43.85684	128	0.888888889
24	44.4791	106	0.736111111
23	45.10432	86	0.597222222
22	45.73236	68	0.472222222
21	46.36308	56	0.388888889
20	46.99634	53.6	0.372222222
19	47.63201	55.2	0.383333333
18	48.26996	59.2	0.411111111
16	49.55216	64.8	0.45
15	50.19615	70.4	0.488888889
12	52.13821	78.4	0.544444444
10	53.44008	81.6	0.566666667
8	54.74657	86	0.597222222
6	56.05673	92	0.638888889
0	60	92.8	0.644444444

**6 min prism 2-- immersed in water for 5 minutes then air dried**

thetain	theta	mV	Normalized
40	34.98304	76	0.550725
36	37.25063	77.8	0.563768
34	38.41445	79.2	0.573913
32	39.59639	84.8	0.614493
30	40.7951	88.8	0.643478
29	41.40034	96	0.695652
28	42.00928	112	0.811594
27	42.62178	138	1
26	43.23769	136	0.985507
25	43.85684	122	0.884058
24	44.4791	112	0.811594
22	45.73236	94	0.681159
21	46.36308	74	0.536232
20	46.99634	62	0.449275
19	47.63201	55	0.398551
18	48.26996	63	0.456522
16	49.55216	68	0.492754
15	50.19615	70	0.507246
12	52.13821	76	0.550725
10	53.44008	79.2	0.573913
6	56.05673	87.2	0.631884
4	57.36963	90.4	0.655072
0	60	95.2	0.689855